Real-world geometric graphs have low average stabbing number

David Eppstein, Michael Goodrich, Lowell Trott

Results

- Constant ply disk systems will have $O(\sqrt{n})$ crossings with a random line
- Graphs that are similar in structure also have this property
 - In particular, we consider boundeddegree multiscale-dispersed graphs

Naturally Associated Disk System

For each vertex in a graph create one disk, centered at the vertex, with radius 1/2 the length of the longest connected edge



Ply of a Disk System

 The largest number of disks that covering some point in the system





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Multiscale-Dispersed Graph

- Graph's naturally associated disk system has constant ply
 - $O(\sqrt{n})$ exceptional disks are allowed



Picture from David Eppstein, Michael Goodrich "Studying (non-planar) road networks through an algorithmic lens"



 Experimental data on U.S.TIGER/Line road network database

Current Work

- Although not true in the worst case, we would like to show that Delaunay triangulations have constant average ply disk systems
 - If so, our conclusions about multiscale-dispersed graphs can be applied to these structures



